

An argon ion beam milling process for native AlO_x layers enabling coherent superconducting contacts

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We present an argon ion beam milling process to remove the native oxide layer forming on aluminum thin films due to their exposure to atmosphere in between lithographic steps. Our cleaning process is readily integrable with conventional fabrication of Josephson junction quantum circuits. From measurements of the internal quality factors of superconducting microwave resonators with and without contacts, we place an upper bound on the residual resistance of an ion beam milled contact of $50 \text{ m}\Omega \mu\text{m}^2$ at a frequency of 4.5 GHz. Resonators for which only 6% of the total foot-print was exposed to the ion beam milling, in areas of low electric and high magnetic fields, showed quality factors above 10^6 in the single photon regime, and no degradation compared to single layer samples. We believe these results will enable the development of increasingly complex superconducting circuits for quantum information processing. *Published by AIP Publishing.*
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The research field of superconducting quantum electronics has been developing at an accelerated pace for the last two decades, and it is now one of the leading candidates for the implementation of quantum mechanical computational machines which could eventually outperform classical computers.¹ On the path to achieving this scientific landmark, microelectronic quantum circuits are required to become increasingly complex, to implement an ever growing set of functionalities, such as fast single and multiple qubit operations,^{2,3} quantum non-demolition readout,⁴⁻⁷ remote qubit entanglement⁸⁻¹¹ and qubit-qubit interactions,¹²⁻¹⁴ or autonomous feedback.^{15,16} Not only are these goals challenging by themselves, but it is paramount that they are achieved without compromising on the quantum coherence of the device.

Several quantum circuit integration approaches are currently pursued with promising results. Flip-chip strategies^{17,18} or complex 2.5D circuit designs^{19,20} have recently shown coherence comparable with state of the art single devices.²¹⁻²³ Their fabrication often requires several lithography steps, involving different clean-room technologies. One of the challenges of integrating different microelectronic fabrication layers²⁴⁻²⁶ is to obtain not only a very good galvanic contact, but also a very high quality factor at microwave frequencies.

Aluminum is one of the most widely used materials for superconducting quantum electronics, thanks to the controllable and convenient growth of the oxide barrier between the electrodes of Josephson junctions, and its relatively low surface dielectric loss tangent.^{27,28} However, aluminum also forms an insulating oxide when exposed to atmosphere, which has to be removed prior to contacting different lithographic layers.

In this letter, we present an argon ion beam milling process to remove the native aluminum oxide, which enables the fabrication of state of the art coherent devices. We show that overlap contacts obtained using ion beam milling did not cause any measurable degradation in the quality factor compared to a continuous metallic film, when embedded into microwave resonators with internal quality factors on the order of 10^6 in the single photon regime.

We perform the argon ion beam milling using the Kaufman ion source connected to the load lock of a PlassysTM MEB 550S shadow evaporation machine at a base pressure in the range of 10^{-7} mbar immediately before the deposition of aluminum thin films. The parameters of the ion source during cleaning are set as follows: 4 sccm argon-gas at a beam voltage of 400 V, an accelerating voltage of 90 V, and an ion current of 15 mA. Between the end of the milling process and the opening of the shutter for the aluminum deposition, the time interval is approximately 300 s. The rate of the aluminum deposition is 0.2 nm/s. All samples are fabricated using an optical lithography lift-off technique employing MicropositTM S1805 resist on double-side polished $330 \mu\text{m}$ thick c-plane sapphire wafers.

We calibrate the duration of the milling process by measuring the decrease in DC resistance of overlap contacts, as shown in Fig. 1(a). After 2 min of milling, the DC contact resistance R_c is smaller than the sheet resistance R_s of a single-layer aluminum film, which defines the measurable upper bound for R_c in our setup. Figure 1(b) shows a SEM image where we can observe the effect of the aggressive cleaning step on the patterned resist: a widening of the strips by $2w_m \lesssim 1 \mu\text{m}$ together with a roughening of the edges. We estimate comparable milling times for the native aluminum oxide layer and the underlying aluminum thin film (see the [supplementary material](#)); therefore, it is crucial not to overetch

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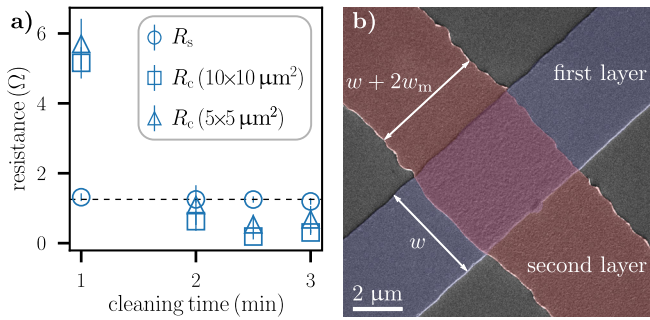


FIG. 1. (a) Measured DC contact resistance R_c at room temperature as a function of cleaning time for 5×5 and $10 \times 10 \mu\text{m}^2$ overlaps. For times longer than 2 min, R_c is below the sheet resistance R_s of a single layer aluminum film. The error bars indicate the standard deviation. Details on the contact resistance measurement are provided in the [supplementary material](#). (b) False colored SEM image of a contact area after 3 min of cleaning and deposition of the second aluminum layer. The second (red) layer shows rough edges due to the aggressive cleaning step performed prior to metal deposition, and a widening of the strip by $2w_m$. From multiple measurements on SEM images we observe that the widening of the strip does not change for milling times between 1 and 3 min, and $2w_m$ can be as large as $1 \mu\text{m}$. The difference in resist height before and after milling for 2.5 min was measured to be less than 20 nm.

the overlapping area of the contacts. Figure 1(b) shows that after 3 min of cleaning, 1 min longer than what is needed for a negligible DC resistance, the first aluminum electrode is still continuous, illustrating the robustness of the process with respect to possible ion beam milling inhomogeneities.

To measure the coherence of the contacts between lithographic layers, we fabricate superconducting resonators with and without overlap contacts and compare their quality factors. The argon ion milling time is 2.5 min. All lithographic layers are done in conventional lift-off technique. Figure 2(a) shows a picture of a $10 \times 15 \text{mm}^2$ sapphire chip with four resonators mounted in a 3D copper waveguide sample holder, following a design that was recently used to perform simultaneous readout of fluxonium qubits.²⁹ The sample holder has a pass band of approximately 1.5 GHz starting from the cutoff frequency of the waveguide at 5.8 GHz. Inside the

band, the reflection from the waveguide to the 50Ω coaxial cables of our measurement setup is below -12 dB . A copper cap closes and shorts the waveguide at a distance of 8 mm (approximately $\lambda/4$ for frequencies in the bandwidth) from the sapphire chip. Silver paste fixes the sapphire chip to the waveguide body, and an indium wire seal ensures good electrical contact as well as tight sealing between the waveguide body and the cap. Two shields machined from a copper/aluminum sandwich and μ -metal around the closed waveguide sample holder provide IR radiation³⁰ and magnetic shielding (see the [supplementary material](#)). The entire assembly is thermally anchored to the base plate of a commercial dilution refrigerator at 25 mK.

In the inset of Fig. 2(a), we show an optical microscope image of one of the measured resonators. For all resonators, the length of the meandering inductor l is 16 mm and its width w is $10 \mu\text{m}$, while the capacitor length d takes the values 1000, 950, 900, and $850 \mu\text{m}$, which distribute the resonant frequencies in a range of 300 MHz around 4.6 GHz. We deliberately design these frequencies below the cutoff frequency of the waveguide to decouple the resonators from the microwave environment and achieve coupling quality factors Q_c in the range of 10^6 [see Fig. 3(a)]. To test the quality factor of the argon ion milled overlap contacts, for half of the measured resonators, the aluminum film of the meander is interrupted in the middle, and reconnected in a second lithographic step using a strip of the same width that we call *bridge*.

Figure 2(b) shows a schematic of our cryogenic measurement setup. A vector network analyzer (VNA) measures the complex response of the resonators. The input signal is in total attenuated by -100 dB , -30 dB at room temperature, and -70 dB distributed at different temperature stages of the cryostat, including the attenuation of the resistive coaxial microwave cables. Two cryogenic circulators provide signal routing and isolation on the output line, respectively. A commercial high electron mobility transistor amplifier on the 1.6 K stage of the cryostat amplifies the outgoing signal by

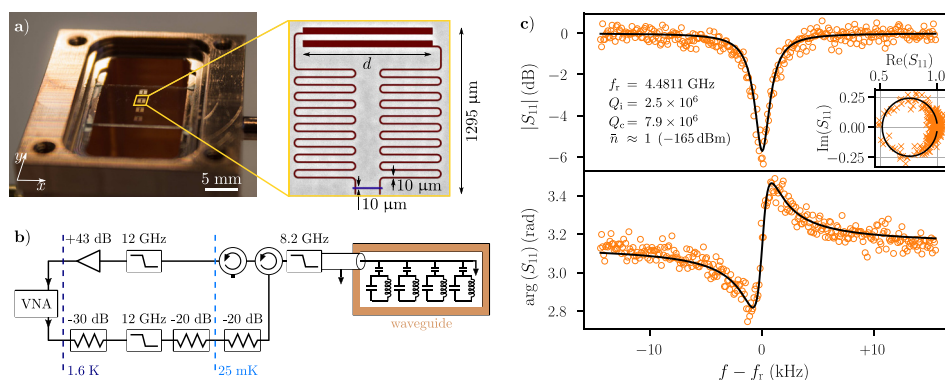


FIG. 2. (a) Photograph of a sample mounted in the copper waveguide sample holder. Each chip holds four resonators. Their dipole moment couples to the TE_{10} mode of the waveguide (E-field parallel to the x direction of the indicated coordinate system). The inset shows an optical microscope image of a resonator in false color. To test the coherent properties of the cleaned contacts, the meander (red) is interrupted in the middle and closed in a second lithographic step by an aluminum thin film of the same width, that we call *bridge* (blue). Varying the length d of the capacitor sweeps the resonant frequencies. All remaining parameters of the design are nominally identical between resonators on one chip. (b) Schematic of the cryogenic measurement setup. A reflection measurement with a vector network analyzer (VNA) characterizes the resonator response. The waveguide is thermally anchored to the mixing chamber plate of a commercial dilution refrigerator. All input and output lines are interrupted by commercial and custom made low pass filters providing at least -30 dB of filtering above 9 GHz. Including cables, the total attenuation on the input lines is -70 dB . (c) Typical measured and fitted (black lines) reflection data of a resonator at an estimated drive power of -165 dBm at the waveguide input, corresponding to an average number of photons $\bar{n} \approx 1$ circulating in the resonator. The fitted values for the resonant frequency f_r , the internal quality factor Q_i , and the coupling quality factor Q_c are indicated in the plot.

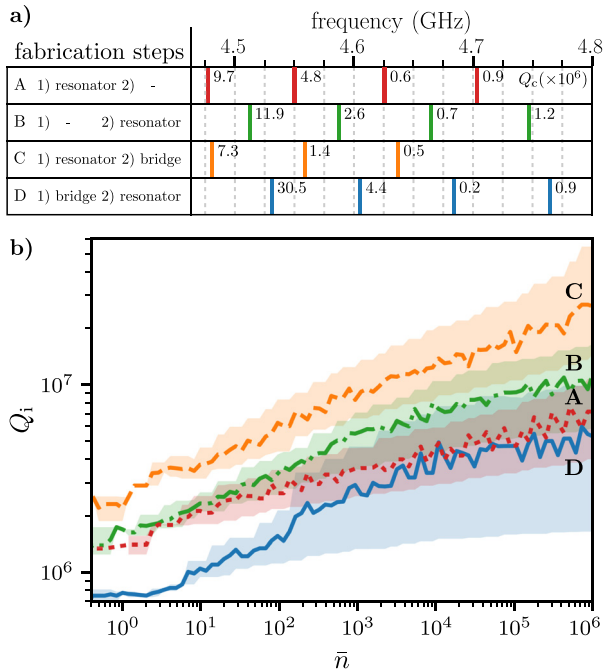


FIG. 3. (a) Overview of all measured samples. The left column shows the order of fabrication, and the right column indicates the resonant frequencies and the corresponding coupling quality factors Q_c in millions. We achieve these weak coupling values by designing resonant frequencies below the cut-off frequency of the waveguide (5.8 GHz). On each sample, the resonators are equally spaced in frequency, approximately 75 MHz apart. For an extensive parameter list, see the [supplementary material](#). The first aluminum layer is deposited with a thickness of 35 nm and the second layer with a thickness of 50 nm. One of the meanders on sample C is interrupted, leaving only three functional resonators. (b) Quality factors of the four investigated samples as a function of the average number of circulating photons \bar{n} . Solid lines indicate the mean internal quality factor Q_i of all fitted resonators of each sample, while the shaded areas show the spread between the highest and the lowest measured Q_i .

+43 dB. At room temperature, a second commercial amplifier adds +60 dB to the signal.

Figure 2(c) shows a typical measured and fitted S_{11} resonator response at an input power of -165 dBm corresponding to an average number of photons circulating in the resonator of $\bar{n} = 4P_{\text{in}}Q_{\text{tot}}^2/\hbar\omega_r^2Q_c \approx 1$. We use a circle fit routine in the complex plane to extract the quality factor and the resonant frequency.³¹

For each sample, Fig. 3 gives an overview of the fabrication sequence, the measured internal quality factors Q_i , the resonant frequencies, and corresponding coupling quality factors Q_c . Notice that the frequencies of the resonators on samples A and C are significantly lower than those of samples B and D. This can be explained by the fact that the entire resonator, except the bridge region, is deposited in lithography step 1 for samples A and C, and in step 2 for B and D. The frequency shift between the two groups of samples is caused by the ion milling step which increases the meander width (see Fig. 1) by $2w_m$, effectively reducing the number of squares, $l/(w + 2w_m)$, for samples B and D, and thereby decreasing the kinetic inductance. The observed shift of approximately 40 MHz could be explained by a widening of the strip $2w_m$ on the order of $1 \mu\text{m}$, which is consistent with the values indicated in Fig. 1(b). Additionally, the milling lowers the geometric inductance of the meander and also

increases the capacitance by reducing the distance between the capacitor pads. However, these two modifications to the resonator geometry will only be on the order of 1%, the resulting changes in resonant frequency will have opposite signs, and they can therefore be neglected. We estimate that the difference between the film thickness of samples A, C (35 nm) and B, D (50 nm) will result in a $\sim 10\%$ change of the kinetic inductance fraction α .³² For sample B, we measured $\alpha = 0.14$ (see Fig. 4), which implies that the frequency shift between samples A, C and B, D, due to the change in kinetic inductance fraction should be less than 5 MHz.

The measured frequency difference between resonators fabricated in the same lithographic step without, and with a contact bridge, is on the order of 10 MHz between samples A and C, and about 20 MHz between samples B and D. Surprisingly, the resonant frequencies of samples with a contact bridge are all higher than the frequencies of the corresponding single layer resonators, indicating a negligible contribution from the kinetic inductance of the overlap contacts. The shift to higher frequencies for resonators on sample C compared to sample A could again be explained by a widening of the bridge during the argon ion milling, consistent with the arguments presented in the previous paragraph. Finally, for sample D, we expect smaller frequencies compared to sample B, however, they are measured to be significantly higher. This shift, observed for samples where the entire area of the resonator was subjected to the ion milling, could also arise from random fluctuations of the width w of structures fabricated in different positions on the wafer. Possible causes for these variations include a non-uniform ion beam profile or inhomogeneities in the UV-beam exposure over the two inch diameter of the wafer.

The solid lines in Fig. 3(b) show the mean Q_i of all resonators for each sample as a function of the average number of circulating photons \bar{n} . The spread between the highest and lowest Q_i of each sample is indicated by the shaded area. We would like to emphasize that the single-layer samples A and B, and sample C, where the cleaning process is only applied to the connecting bridge, show internal quality factors larger than 10^6 in the single photon regime. Remarkably, we measure the highest average Q_i on the resonators of sample C

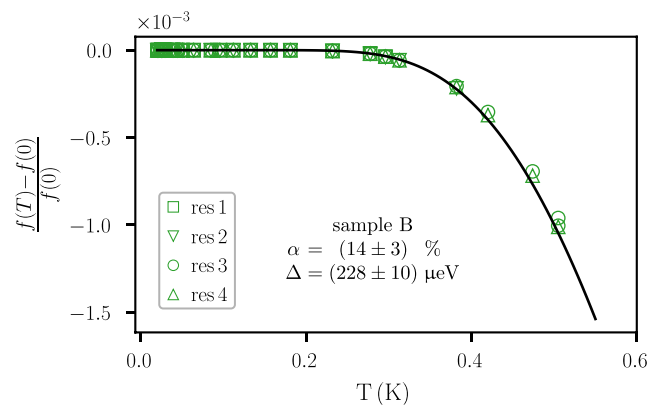


FIG. 4. Measurement of the kinetic inductance fraction α . The symbols show the relative shift of the resonant frequency of the four resonators on sample B as a function of temperature. The data of each resonator are fitted using Eq. (1). The black line shows the model using the average values of the four individual fits: $\alpha = (14 \pm 3)\%$ and $\Delta = 228 \pm 10 \mu\text{eV}$.

which include an ion beam milled contact bridge. From the mean internal quality factors of samples with a bridge (C, D) we extract an upper bound on the residual resistance of the contacts of $50 \text{ m}\Omega \mu\text{m}^2$ (see the [supplementary material](#)). From 3D finite elements simulations we extract the sum of the participation ratios of the metal-substrate and metal-air interfaces of the resonator to be $p_{\text{tot}} = 1.8 \times 10^{-4}$ (see the [supplementary material](#)), which is smaller than in coplanar geometries, due to the larger mode volume of the waveguide sample holder. This allows us to extract a surface dielectric loss tangent $\tan \delta = (p \overline{Q}_i)^{-1} = 4 \times 10^{-3}$, which is in the range of commonly reported values.²⁸

A potential inhomogeneity of the argon ion beam could have caused stronger milling of sample D and a degradation of the substrate,³³ thereby explaining the lower quality factors of all resonators of sample D, compared to those of sample B.

To measure the kinetic inductance fraction α of sample B, for which the entire surface of the resonators was subjected to the milling, we measure the temperature dependence of the resonant frequencies. The measured change of the resonant frequency as a function of temperature (see Fig. 4) is modeled using the following equation:^{32,34}

$$df(T)/f_r = -\alpha/2\sqrt{\pi\Delta/2k_B T} \exp(-\Delta/k_B T), \quad (1)$$

where the kinetic inductance fraction $\alpha = L_{\text{kin}}/L_{\text{tot}}$ and the superconducting gap Δ are used as fit parameters.

The fit is performed for all four resonators of sample B individually. Taking the average of all fitted parameters yields mean values of $\alpha = (14 \pm 3)\%$, and $\Delta = (228 \pm 10) \mu\text{eV}$ which corresponds to a BCS critical temperature of $(1.5 \pm 0.1) \text{ K}$. Therefore, we do not observe any change in the intrinsic properties of the aluminum thin film deposited after the ion beam milling process compared to standard aluminum thin films.³²

We have demonstrated an argon ion beam milling process for the removal of the native oxide layer forming on aluminum thin films. Measurements of superconducting microwave resonators in the single photon regime show no degradation of Q_i at a level of 10^6 when the milling process is used on a small area of the superconducting circuit. Very recently, similar bounds on coherence were reported for overlap Josephson junctions³⁵ and contacts.³³ If the milling is performed on the entire area of the resonator it induces at most a factor of two degradation in Q_i . These results enable the development of increasingly complex superconducting circuit designs with several interconnected lithographic layers, without compromising their coherence properties, thereby opening the way to the integration of very different and often complementary quantum systems such as Josephson junctions and superconducting high kinetic inductance nanowires,^{36,37} or mesoscopic semiconductor structures.^{38–40}

See [supplementary material](#) for detailed information on the measurement of the DC contact resistance, the calculation of the residual resistance of the overlap contacts, extended parameters of the resonator characterization, the native oxide milling rate, a description for the estimation of the interface participation ratios, and details on the shielding of our resonator samples.

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¹M. H. Devoret and R. J. Schoelkopf, *Science* **339**, 1169 (2013).

²J. H. Plantenberg, P. C. de Groot, C. J. P. M. Harmans, and J. E. Mooij, *Nature* **447**, 836 (2007).

³R. Barends, J. Kelly, A. Megrant, A. Veitia, D. Sank, E. Jeffrey, T. C. White, J. Mutus, A. G. Fowler, B. Campbell, Y. Chen, Z. Chen, B. Chiaro, A. Dunsworth, C. Neill, P. O'Malley, P. Roushan, A. Vainsencher, J. Wenner, A. N. Korotkov, A. N. Cleland, and J. M. Martinis, *Nature* **508**, 500 (2014).

⁴A. Wallraff, D. I. Schuster, A. Blais, L. Frunzio, R.-S. Huang, J. Majer, S. Kumar, S. M. Girvin, and R. J. Schoelkopf, *Nature* **431**, 162 (2004).

⁵M. A. Castellanos-Beltran and K. W. Lehnert, *Appl. Phys. Lett.* **91**, 083509 (2007).

⁶R. Vijay, D. H. Slichter, and I. Siddiqi, *Phys. Rev. Lett.* **106**, 110502 (2011).

⁷B. Abdo, F. Schackert, M. Hatridge, C. Rigetti, and M. Devoret, *Appl. Phys. Lett.* **99**, 162506 (2011).

⁸D. Ristè, M. Dukalski, C. A. Watson, G. de Lange, M. J. Tiggelman, Y. M. Blanter, K. W. Lehnert, R. N. Schouten, and L. DiCarlo, *Nature* **502**, 350 (2013).

⁹L. Steffen, Y. Salathe, M. Oppliger, P. Kurpiers, M. Baur, C. Lang, C. Eichler, G. Puebla-Hellmann, A. Fedorov, and A. Wallraff, *Nature* **500**, 319 (2013).

¹⁰J. M. Chow, J. M. Gambetta, E. Magesan, D. W. Abraham, A. W. Cross, B. R. Johnson, N. A. Masluk, C. A. Ryan, J. A. Smolin, S. J. Srinivasan, and M. Steffen, *Nat. Commun.* **5**, 4015 (2014).

¹¹N. Roch, M. E. Schwartz, F. Motzoi, C. Macklin, R. Vijay, A. W. Eddins, A. N. Korotkov, K. B. Whaley, M. Sarovar, and I. Siddiqi, *Phys. Rev. Lett.* **112**, 170501 (2014).

¹²A. J. Berkley, H. Xu, R. C. Ramos, M. A. Gubrud, F. W. Strauch, P. R. Johnson, J. R. Anderson, A. J. Dragt, C. J. Lobb, and F. C. Wellstood, *Science* **300**, 1548 (2003).

¹³M. Steffen, M. Ansmann, R. C. Bialczak, N. Katz, E. Lucero, R. McDermott, M. Neeley, E. M. Weig, A. N. Cleland, and J. M. Martinis, *Science* **313**, 1423 (2006).

¹⁴J. Majer, J. M. Chow, J. M. Gambetta, J. Koch, B. R. Johnson, J. A. Schreier, L. Frunzio, D. I. Schuster, A. A. Houck, A. Wallraff, A. Blais, M. H. Devoret, S. M. Girvin, and R. J. Schoelkopf, *Nature* **449**, 443 (2007).

¹⁵S. Shankar, M. Hatridge, Z. Leghtas, K. Sliwa, A. Narla, U. Vool, S. M. Girvin, L. Frunzio, M. Mirrahimi, and M. H. Devoret, *Nature* **504**, 419 (2013).

¹⁶K. Geerlings, Z. Leghtas, I. M. Pop, S. Shankar, L. Frunzio, R. J. Schoelkopf, M. Mirrahimi, and M. H. Devoret, *Phys. Rev. Lett.* **110**, 120501 (2013).

¹⁷Z. K. Mineev, K. Serniak, I. M. Pop, Z. Leghtas, K. Sliwa, M. Hatridge, L. Frunzio, R. J. Schoelkopf, and M. H. Devoret, *Phys. Rev. Appl.* **5**, 044021 (2016).

¹⁸T. Brecht, M. Reagor, Y. Chu, W. Pfaff, C. Wang, L. Frunzio, M. H. Devoret, and R. J. Schoelkopf, *Appl. Phys. Lett.* **107**, 192603 (2015).

¹⁹J. Kelly, R. Barends, A. G. Fowler, A. Megrant, E. Jeffrey, T. C. White, D. Sank, J. Y. Mutus, B. Campbell, Y. Chen, Z. Chen, B. Chiaro, A. Dunsworth, I.-C. Hoi, C. Neill, P. J. J. O'Malley, C. Quintana, P. Roushan, A. Vainsencher, J. Wenner, A. N. Cleland, and J. M. Martinis, *Nature* **519**, 66 (2015).

²⁰D. Ristè, S. Poletto, M.-Z. Huang, A. Bruno, V. Vesterinen, O.-P. Saira, and L. DiCarlo, *Nat. Commun.* **6**, 6983 (2015).

²¹H. Paik, D. I. Schuster, L. S. Bishop, G. Kirchmair, G. Catelani, A. P. Sears, B. R. Johnson, M. J. Reagor, L. Frunzio, L. I. Glazman, S. M. Girvin, M. H. Devoret, and R. J. Schoelkopf, *Phys. Rev. Lett.* **107**, 240501 (2011).

- ²²C. Rigetti, J. M. Gambetta, S. Poletto, B. L. T. Plourde, J. M. Chow, A. D. Córcoles, J. A. Smolin, S. T. Merkel, J. R. Rozen, G. A. Keefe, M. B. Rothwell, M. B. Ketchen, and M. Steffen, *Phys. Rev. B* **86**, 100506 (2012).
- ²³R. Barends, J. Kelly, A. Megrant, D. Sank, E. Jeffrey, Y. Chen, Y. Yin, B. Chiaro, J. Mutus, C. Neill, P. O'Malley, P. Roushan, J. Wenner, T. C. White, A. N. Cleland, and J. M. Martinis, *Phys. Rev. Lett.* **111**, 080502 (2013).
- ²⁴M. Sandberg, M. R. Vissers, J. S. Kline, M. Weides, J. Gao, D. S. Wisbey, and D. P. Pappas, *Appl. Phys. Lett.* **100**, 262605 (2012).
- ²⁵M. R. Vissers, M. P. Weides, J. S. Kline, M. Sandberg, and D. P. Pappas, *Appl. Phys. Lett.* **101**, 022601 (2012).
- ²⁶J. Braumüller, J. Cramer, S. Schlör, H. Rotzinger, L. Radtke, A. Lukashenko, P. Yang, S. T. Skacel, S. Probst, M. Marthaler, L. Guo, A. V. Ustinov, and M. Weides, *Phys. Rev. B* **91**, 054523 (2015).
- ²⁷A. D. O'Connell, M. Ansmann, R. C. Bialczak, M. Hofheinz, N. Katz, E. Lucero, C. McKenney, M. Neeley, H. Wang, E. M. Weig, A. N. Cleland, and J. M. Martinis, *Appl. Phys. Lett.* **92**, 112903 (2008).
- ²⁸C. Wang, C. Axline, Y. Y. Gao, T. Brecht, Y. Chu, L. Frunzio, M. H. Devoret, and R. J. Schoelkopf, *Appl. Phys. Lett.* **107**, 162601 (2015).
- ²⁹A. Kou, W. C. Smith, U. Vool, I. M. Pop, K. M. Sliwa, M. H. Hatridge, L. Frunzio, and M. H. Devoret, e-print [arXiv:1705.05712](https://arxiv.org/abs/1705.05712) [quant-ph].
- ³⁰R. Barends, J. Wenner, M. Lenander, Y. Chen, R. C. Bialczak, J. Kelly, E. Lucero, P. O'Malley, M. Mariantoni, D. Sank, H. Wang, T. C. White, Y. Yin, J. Zhao, A. N. Cleland, J. M. Martinis, and J. J. A. Baselmans, *Appl. Phys. Lett.* **99**, 113507 (2011).
- ³¹S. Probst, F. B. Song, P. A. Bushev, A. V. Ustinov, and M. Weides, *Rev. Sci. Instrum.* **86**, 024706 (2015).
- ³²J. Gao, "The physics of superconducting microwave resonators," Ph.D. dissertation (California Institute of Technology, 2008).
- ³³A. Dunsworth, A. Megrant, C. Quintana, Z. Chen, R. Barends, B. Burkett, B. Foxen, Y. Chen, B. Chiaro, A. Fowler, R. Graff, E. Jeffrey, J. Kelly, E. Lucero, J. Y. Mutus, M. Neeley, C. Neill, P. Roushan, D. Sank, A. Vainsencher, J. Wenner, T. C. White, and J. M. Martinis, *Appl. Phys. Lett.* **111**, 022601 (2017).
- ³⁴J. P. Turneaure, J. Halbritter, and H. A. Schwettman, *J. Supercond.* **4**, 341 (1991).
- ³⁵X. Wu, J. L. Long, H. S. Ku, R. E. Lake, M. Bal, and D. P. Pappas, *Appl. Phys. Lett.* **111**, 032602 (2017).
- ³⁶J. E. Mooij and Y. V. Nazarov, *Nat. Phys.* **2**, 169 (2006).
- ³⁷O. V. Astafiev, L. B. Ioffe, S. Kafanov, Y. A. Pashkin, K. Y. Arutyunov, D. Shahar, O. Cohen, and J. S. Tsai, *Nature* **484**, 355 (2012).
- ³⁸J.-P. Cleuziou, W. Wernsdorfer, V. Bouchiat, T. Ondarçuhu, and M. Monthieux, *Nat. Nanotechnol.* **1**, 53 (2006).
- ³⁹T. W. Larsen, K. D. Petersson, F. Kuemmeth, T. S. Jespersen, P. Krogstrup, J. Nygård, and C. M. Marcus, *Phys. Rev. Lett.* **115**, 127001 (2015).
- ⁴⁰G. de Lange, B. van Heck, A. Bruno, D. J. van Woerkom, A. Geresdi, S. R. Plissard, E. P. A. M. Bakkers, A. R. Akhmerov, and L. DiCarlo, *Phys. Rev. Lett.* **115**, 127002 (2015).